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## APPENDIX A

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**Methods for Daily Climate Index Development & Additional 2015  
Water Quality Data**



## Daily Climate Index Development & Relationship with Schmidt Stability

To determine the conditions that dictate the duration of stratification in Kentuck Lake each year, a Daily Climate Index (DCI) using daily average air temperature, daily average wind speed, and daily average wind direction was developed and compared against the lake's thermal stability. Thermal stability is a measure of how much work is needed to mix the entire water column of water and is measured in g/cm. A stability value of 0 indicates the entire water column is of uniform temperature and no work is needed to mix it. A higher stability value indicates that a strong temperature/density gradient exists between surface and bottom waters and that more work or energy is needed to mix them together. The goal of this analysis is to determine the conditions that lead to the onset of stratification, the conditions that maintain stratification, and conditions that result in mid-summer mixing events.

Kentuck Lake's maximum fetch length is oriented from southwest to northeast meaning that southwest and northeast winds will impart the highest energy across the lake and most likely to result in mixing events. In the DCI, if daily wind direction was equal to or between 202.5° and 247.5° (west-southwest to south-southwest) or 22.5° and 67.5° (north-northeast to east-northeast) wind speed was multiplied by a factor of 1.75. The DCI and Schmidt Stability Index were calculated using the following equations:

Daily Climate Index (DCI):

$$DCI = \frac{T_z}{\sqrt{W_z * W_d}}$$

Where

$T_z$  = Daily average air temperature (°C)

$W_z$  = Daily average wind speed (kph)

$W_d$  = Wind direction factor.  $W_d = 1.75$  if  $22.5^\circ \leq$  daily wind direction  $\leq 67.5^\circ$  or  $202.5^\circ \leq$  daily wind direction  $\leq 247.5^\circ$ ; otherwise  $W_d = 1$

Schmidt Stability Index:

$$S = \frac{1}{A_0} \sum_{z=0}^{z=m} (p_z - p^*)(z - z_p)(A_z)(\Delta z)$$

Where

$A_0$  = the area of the water body (cm<sup>2</sup>)

$A_z$  = lake area at depth  $z$  (cm)

$p_z$  = density as calculated from temperature (g/cm<sup>2</sup>)

$p^*$  = lake's mean density (g/cm<sup>2</sup>)

$z_p$  = depth at which mean density is found (cm)

$m$  = maximum depth of the lake (cm)

$\Delta z$  = depth interval of measurements (cm)

To explore both short and longer-term effects of weather on Kentuck Lake's thermal stability, the mean DCI value was calculated over 1, 2, 3, 5, 7, 10, and 15 days prior to the collection of lake temperature data. A Pearson pairwise correlation using the 2014 and 2015 DCI and stability data collected from spring turnover through the first mid-summer complete mixing event was used to determine which mean DCI period was the best predictor of thermal stability. The results of the Pearson pairwise correlation indicated that the 7-day mean DCI value was the strongest predictor of thermal stability in Kentuck Lake with an  $r$  value of 0.927 (Table 1).

**Table 1. Pearson pairwise correlation tables of established mean 2014 and 2015 Daily Climate Index periods and Schmidt stability from spring turnover to the first summer mixing event (left) and post-summer mixing event (right).** Values represent the correlation  $r$  values.

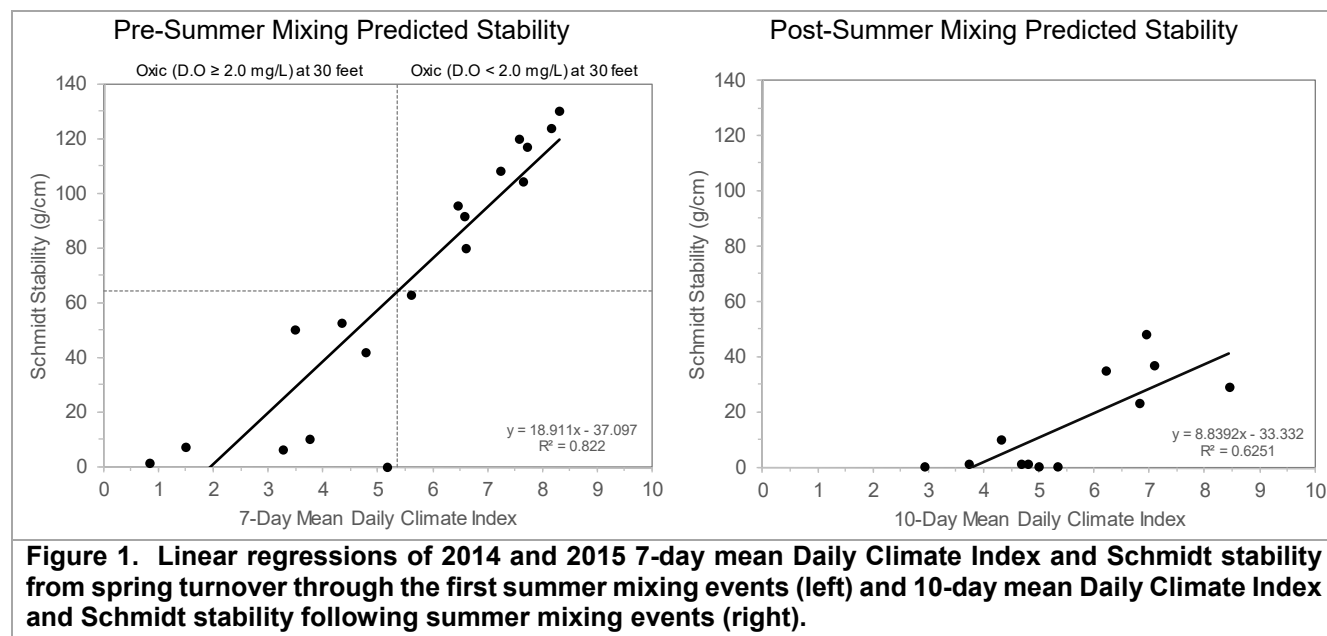
Spring Turnover to Summer Mixing Event		Post-Summer Mixing Event	
DCI Time Period	Schmidt Stability (g/cm)	DCI Time Period	Schmidt Stability (g/cm)
1-day Mean DCI Value	0.747	1-day Mean DCI Value	0.610
2-day Mean DCI Value	0.825	2-day Mean DCI Value	0.732
3-day Mean DCI Value	0.878	3-day Mean DCI Value	0.745
5-day Mean DCI Value	0.910	5-day Mean DCI Value	0.748
7-day Mean DCI Value	0.927	7-day Mean DCI Value	0.748
10-day Mean DCI Value	0.893	10-day Mean DCI Value	0.802
12-day Mean DCI Value	0.839	12-day Mean DCI Value	0.744
15-day Mean DCI Value	0.789	15-day Mean DCI Value	0.639

Linear regression of the 2014 and 2015 7-day mean DCI and thermal stability data from spring turnover through the first mid-summer mixing event illustrates a good relationship with an  $R^2$  of 0.822 (Figure 1). Another Pearson pairwise correlation of 2015 dissolved oxygen recorded at two-foot intervals from site 1 and epilimnetic total phosphorus concentrations indicated that dissolved oxygen at 30 feet was the best predictor of epilimnetic phosphorus concentration ( $r$  value -0.742). Plotting 2014 and 2015 dissolved oxygen at 30 feet against thermal stability revealed an exponential relationship ( $R^2 = 0.858$ ), with 30 feet developing anoxia (dissolved oxygen < 2.0 mg/L) when thermal stability is approximately 64 g/cm. A thermal stability of 64 g/cm develops when the 7-day mean DCI is approximately 5.3 (Figure 1).

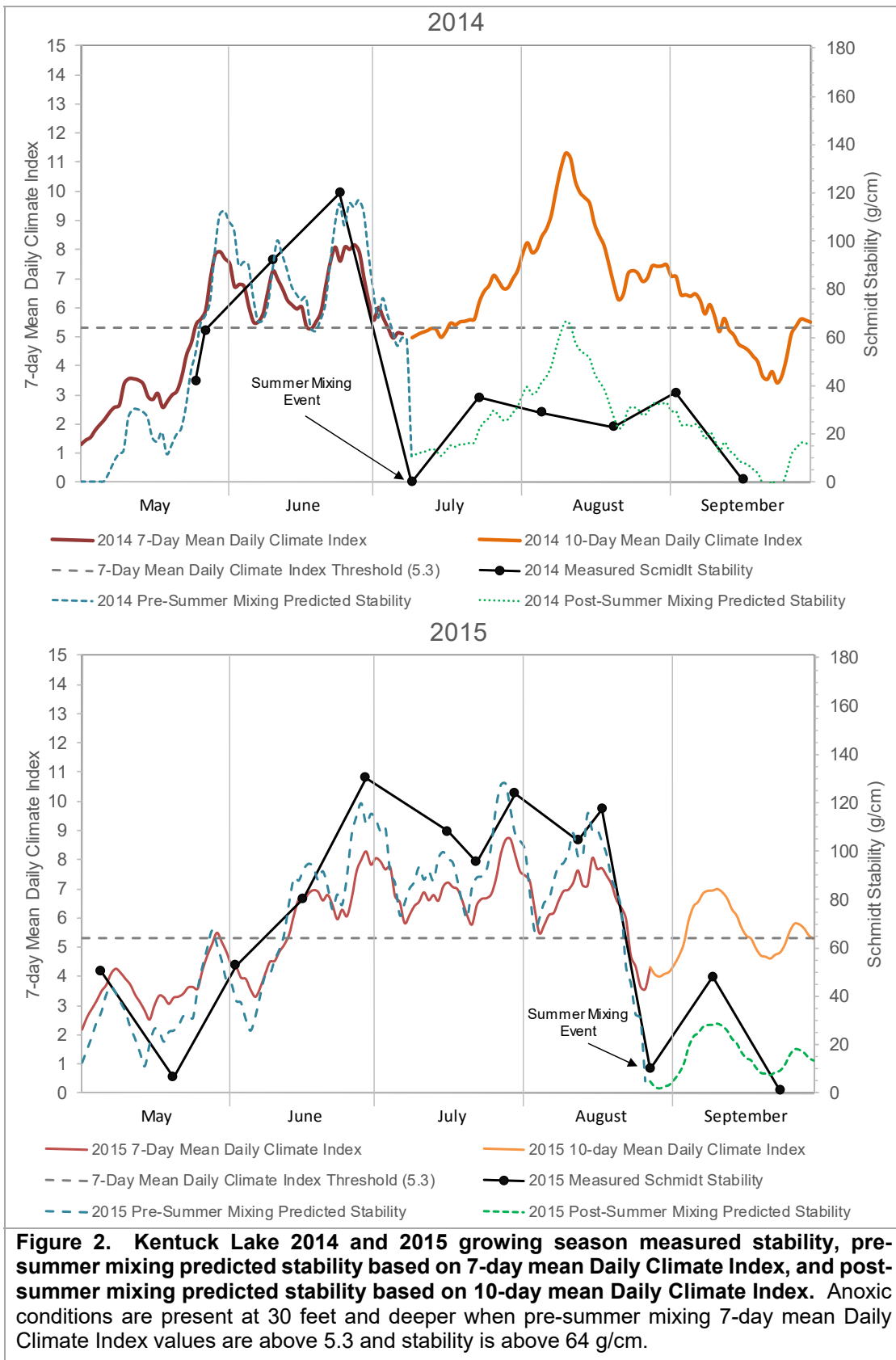
If the 7-day mean DCI is maintained at or above 5.3, thermal stability will increase and anoxic conditions will be maintained that will lead to significant release of nutrients from bottom sediments and an increase in epilimnetic phosphorus concentration. However, if the 7-day mean DCI declines to 5.3 after the lake has already thermally stratified, a complete mixing event will likely occur. In 2014, thermal stability reached 64 g/cm in late-May and stability reached a maximum of 120 g/cm in late-June (Figure 2). The 7-day mean DCI declined to below the 5.3 threshold in early-July and a complete mixing event was observed. In 2015, thermal stability reached 64g/cm in mid-June and continued to increase with the 7-day mean DCI (Figure 2). From early- to mid-July, the 7-day mean DCI began to decline from 7.8 to 5.8 causing a decline in thermal stability and significant deepening of the epilimnion but did not cause a complete mixing event. It was not until late-August when the 7-day mean DCI dropped below 5.3 and reaching a minimum of 3.7 that a complete mixing event occurred.

Climatic conditions are a good predictor of thermal stability and the duration of anoxia in Kentuck Lake from spring turnover through the first summer mixing event; however, this same predictive

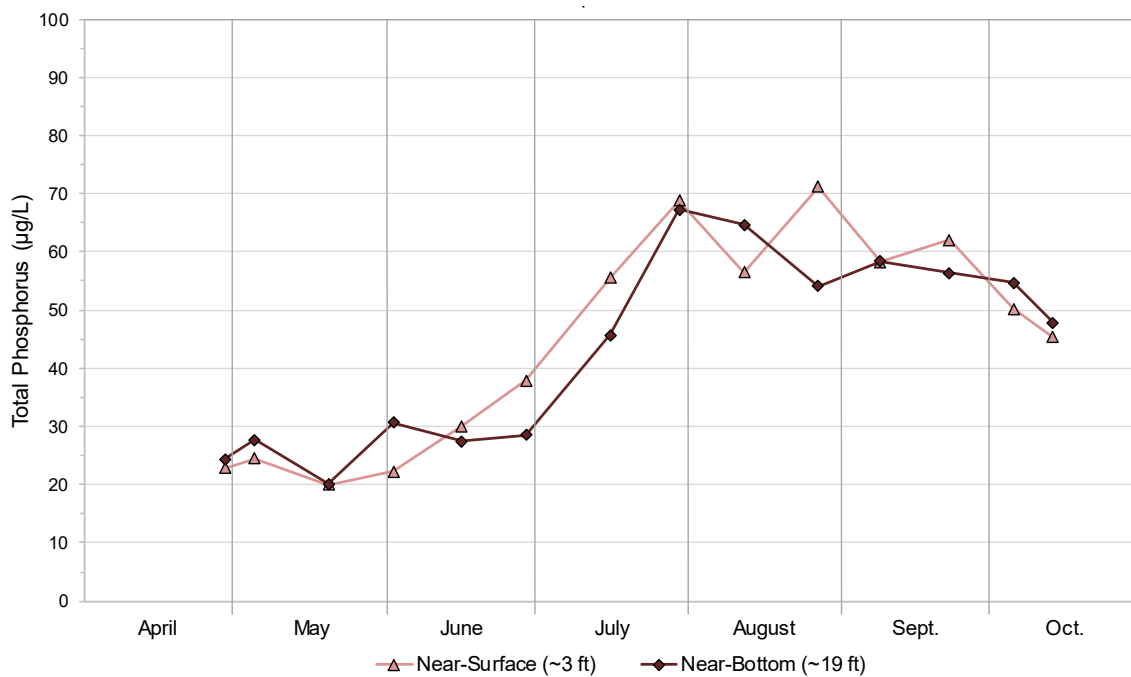
model does not accurately predict thermal stability based on climatic conditions following a complete summer mixing event. While a thermal stability value of 0 indicates a uniform temperature throughout the entire water column, it does provide any information on the temperature of the water. While thermal stability is 0 during both spring turnover and during summer mixing events, water column temperature is much warmer in summer. With water temperatures throughout the water column now similar to summer air temperatures, a strong thermal gradient can no longer be created and thermal stability remains relatively low. Following the 2014 and 2015 summer mixing events, thermal stability never exceeded 50 g/cm despite higher 7-day mean DCI values.



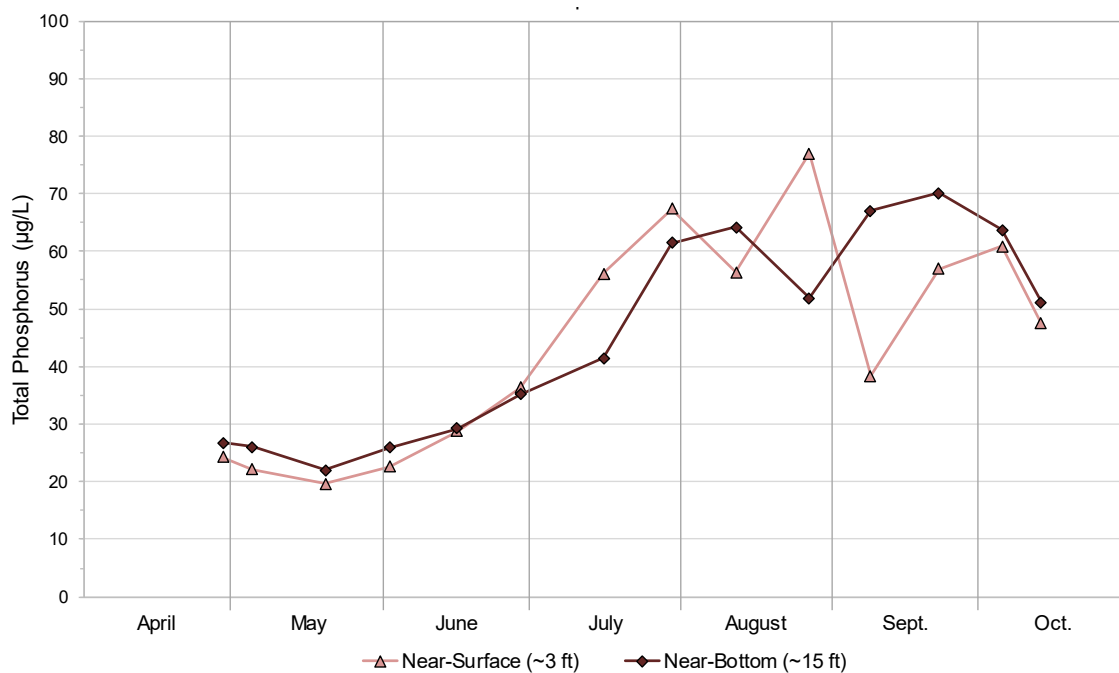
Using 2014 and 2015 post-summer mixing climatic and stability data, another predictive model created to predict stability following a summer mixing event. A Pearson pairwise correlation indicated that the 10-day mean DCI was the best predictor of thermal stability following a mixing event with an  $r$  value 0.802 (Table 1). The linear regression of the post-summer mixing 10-day DCI and stability data are displayed in Figure 1, and Figure 2 illustrates that this additional model is a better predictor of stability following a summer mixing event.



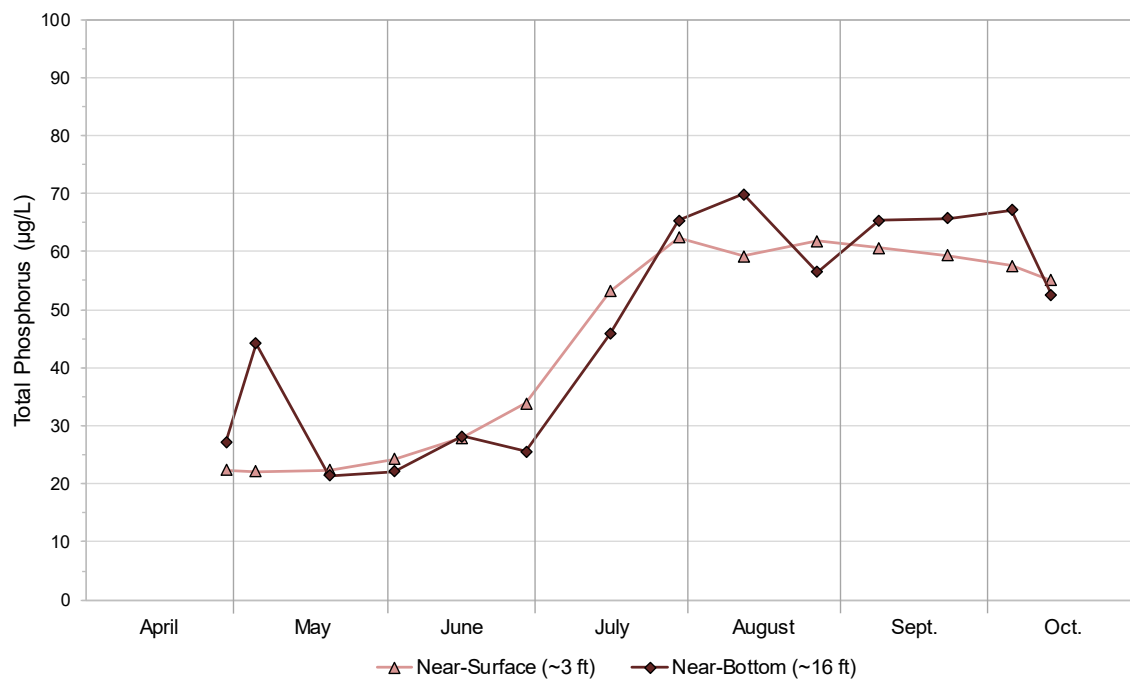
### Kentuck Lake 2015 Additional Water Quality Data



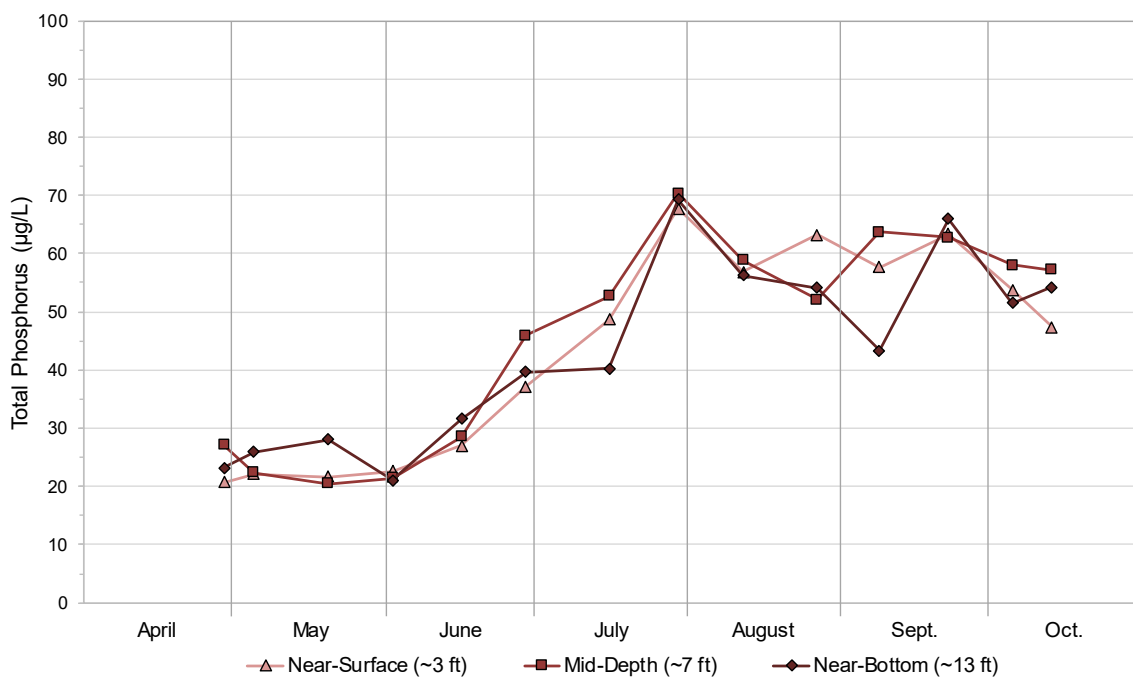
**Figure 3. Kentuck Lake 2015 near-surface and near-bottom total phosphorus concentrations from site 2.**



**Figure 4. Kentuck Lake 2015 near-surface and near-bottom total phosphorus concentrations from site 3.**

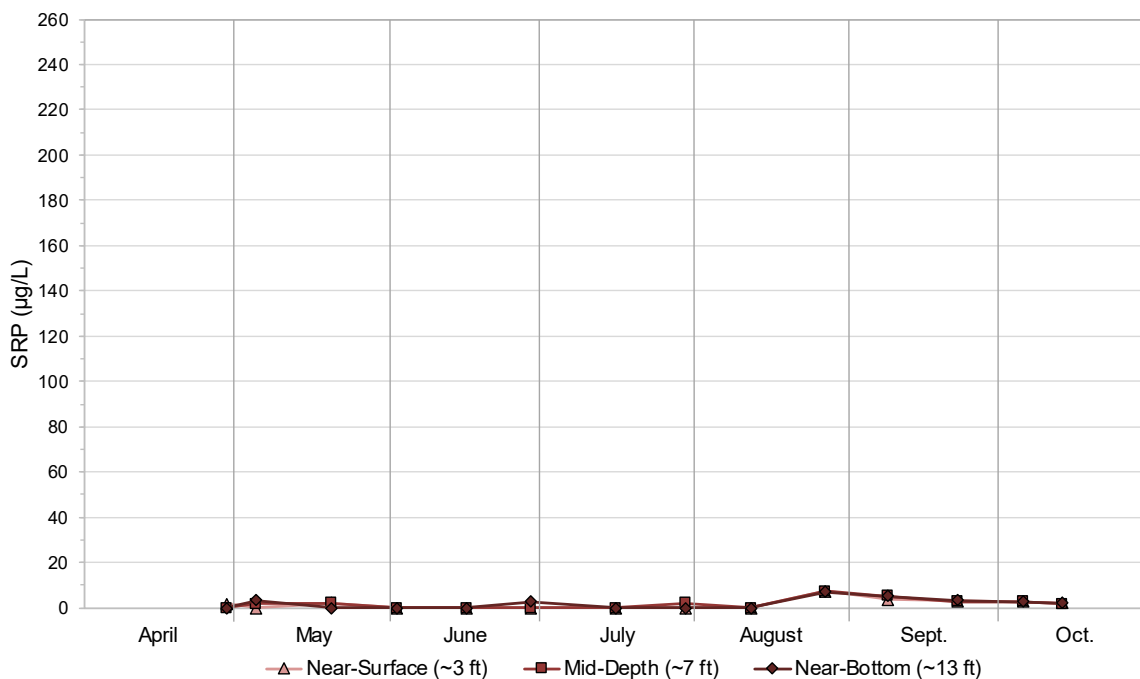


**Figure 5. Kentuck Lake 2015 near-surface and near-bottom total phosphorus concentrations from site 4.**



**Figure 6. Kentuck Lake 2015 near-surface, mid-depth, and near-bottom total phosphorus concentrations from site 5.**





**Figure 7. Kentuck Lake 2015 near-surface and near-bottom soluble reactive phosphorus concentrations from site 5.**

**Table 2. Kentuck Lake 2015 dominant phytoplankton taxa.** Analysis completed by Jim Kreitlow (WDNR).

Date	Depth (ft)	Temp. (°C)	D.O. (mg/L)	Dominant Taxa	Type
4/29/2015	3.0*	8.7	11.7	<i>Asterionella formosa</i> <i>Gymnodinium</i> sp.	Diatom Dinoflagellate
	20.0*	8.7	11.5	No Dominant Taxa	
	38.0*	7.2	8.6	<i>Asterionella formosa</i> <i>Cryptomonas</i> sp. <i>Fragilaria crotonensis</i>	Diatom Cryptomonad Diatom
5/5/2015	3.0	14.0	10.8	No Dominant Taxa	
	20.0*	12.2	10.2	No Dominant Taxa	
	37.0*	7.7	4.6	<i>Trachelomonas</i> sp.	Euglenid
5/20/2015	3.0*	13.9	10.0	<i>Asterionella formosa</i> <i>Dinobyron</i> sp. <i>Fragilaria crotonensis</i> <i>Synedra ulna</i>	Diatom Golden Brown Diatom Diatom
	25.0*	13.2	10.0	<i>Asterionella formosa</i>	Diatom

				<i>Dictyosphaerium</i> sp. <i>Dinobyron</i> sp.	Green Golden Brown
	37.0*	13.1	9.7	<i>Asterionella formosa</i> <i>Dinobyron</i> sp. <i>Mallomonas</i> sp. <i>Synedra ulna</i>	Diatom Golden Brown Golden Brown Diatom
6/2/2015	3.0*	17.4	9.7	<i>Asterionella formosa</i> <i>Dinobyron</i> sp.	Diatom Golden Brown
	20.0*	17.0	9.6	<i>Asterionella formosa</i> <i>Dinobyron</i> sp. <i>Fragilaria crotonensis</i>	Diatom Golden Brown Diatom
	37.0*	13.1	9.0	<i>Asterionella formosa</i> <i>Melosira</i> sp. <i>Trachelomonas</i> sp.	Diatom Diatom Euglenid
6/16/2015	3.0	19.3	10.0	<i>Anabaena</i> spp. <i>Cryptomonas</i> sp. <i>Gloeotrichia echinulata</i>	Blue-green Cryptomonad Blue-green
	28.0*	17.2	1.7	<i>Asterionella formosa</i> <i>Fragilaria crotonensis</i> <i>Melosira</i> sp.	Diatom Diatom Diatom
	37.0*	12.6	0.0	<i>Asterionella formosa</i> <i>Fragilaria crotonensis</i>	Diatom Diatom
6/29/2015	3.0	23.6	11.7	<i>Anabaena</i> spp. <i>Aphanizomenon flos-aquae</i>	Blue-green Blue-green
	26.0*	18.3	1.0	<i>Dictyosphaerium</i> sp.	Green
	37.0*	12.9	0.0	No Dominant Taxa	
7/16/2015	3.0	23.1	10.5	<i>Anabaena</i> spp. <i>Gloeotrichia echinulata</i>	Blue-green Blue-green
	21.0*	19.9	1.2	No Dominant Taxa	
	37.0*	14.0	0.0	<i>Melosira</i> sp. <i>Stephanodiscus</i> sp.	Diatom Diatom
7/30/2015	3.0	23.0	7.9	<i>Anabaena</i> spp. <i>Aphanizomenon flos-aquae</i>	Blue-green Blue-green

				<i>Ceratium hirundinella</i>	Dinoflagellate
	30.0	16.8	0.2	<i>Anabaena</i> spp. <i>Aphanizomenon flos-aquae</i> <i>Ceratium hirundinella</i> <i>Gloeotrichia echinulata</i>	Blue-green Blue-green Dinoflagellate Blue-green
	35.0	13.0	0.0	<i>Anabaena</i> spp.	Blue-green
8/12/2015	3.0	21.5	8.4	<i>Anabaena</i> spp. <i>Aphanizomenon flos-aquae</i>	Blue-green Blue-green
	31.0	14.6	0.1	<i>Anabaena</i> spp. <i>Stephanodiscus</i> sp.	Blue-green Diatom
	36.0	13.3	0.4	<i>Anabaena</i> spp. <i>Stephanodiscus</i> sp.	Blue-green Diatom
8/27/2015	3.0	17.9	11.0	<i>Anabaena</i> spp. <i>Dictyosphaerium</i> sp. <i>Fragilaria crotonensis</i> <i>Mallomonas</i> sp. <i>Stephanodiscus</i> sp. <i>Synedra</i> sp.	Blue-green Green Diatom Golden Brown Diatom Diatom
	20.0	17.5	8.3	<i>Anabaena</i> spp. <i>Fragilaria crotonensis</i> <i>Gomposphaeria</i> sp. <i>Melosira</i> sp. <i>Stephanodiscus</i> sp. <i>Synedra</i> sp.	Blue-green Diatom Blue-green Diatom Diatom Diatom
	36.0	17.1	7.5	<i>Dictyosphaerium</i> sp. <i>Euastrum</i> sp. <i>Fragilaria crotonensis</i> <i>Gomposphaeria</i> sp. <i>Pediastrum boryanum</i> <i>Stephanodiscus</i> sp. <i>Synedra</i> sp.	Green Green Diatom Blue-green Green Diatom Diatom
9/9/2015	3.0	21.4	9.7	<i>Anabaena</i> spp. <i>Aphanizomenon flos-aquae</i> <i>Dictyosphaerium</i> sp. <i>Fragilaria crotonensis</i> <i>Stephanodiscus</i> sp.	Blue-green Blue-green Green Diatom Diatom
	19.0	18.9	0.6	<i>Anabaena</i> spp.	Blue-green

				<i>Aphanizomenon flos-aquae</i>	Blue-green
				<i>Fragilaria crotonensis</i>	Diatom
				<i>Synedra</i> sp.	Diatom
	37.0*	17.8	0.0	<i>Fragilaria crotonensis</i>	Diatom
				<i>Synedra</i> sp.	Diatom
9/23/2015	3.0	17.8	10.6	<i>Anabaena</i> spp.	Blue-green
				<i>Aphanizomenon flos-aquae</i>	Blue-green
				<i>Cryptomonas</i> sp.	Cryptomonad
				<i>Gomphosphaeria</i> sp.	Blue-green
				<i>Stephanodiscus</i> sp.	Diatom
	20.0	17.8	10.2	<i>Anabaena</i> spp.	Blue-green
				<i>Aphanizomenon flos-aquae</i>	Blue-green
				<i>Gomphosphaeria</i> sp.	Blue-green
				<i>Stephanodiscus</i> sp.	Diatom
	37.0	17.6	6.4	<i>Anabaena</i> spp.	Blue-green
				<i>Aphanizomenon flos-aquae</i>	Blue-green
				<i>Gomphosphaeria</i> sp.	Blue-green
				<i>Stephanodiscus</i> sp.	Diatom
10/6/2015	3.0	13.9	10.2	<i>Anabaena</i> spp.	Blue-green
				<i>Aphanizomenon flos-aquae</i>	Blue-green
				<i>Coelosphaerium</i> sp.	Blue-green
				<i>Fragilaria crotonensis</i>	Diatom
	20.0	13.8	10.0	<i>Dictyosphaerium</i> sp.	Green
				<i>Fragilaria crotonensis</i>	Diatom
				<i>Gomphosphaeria</i> sp.	Blue-green
				<i>Melosira</i> sp.	Diatom
				<i>Stephanodiscus</i> sp.	Diatom
	37.0	13.8	10.2	<i>Dictyosphaerium</i> sp.	Green
				<i>Fragilaria crotonensis</i>	Diatom
				<i>Gomphosphaeria</i> sp.	Blue-green
				<i>Melosira</i> sp.	Diatom
				<i>Stephanodiscus</i> sp.	Diatom
10/14/2015	3.0	12.2	11.6	<i>Dictyosphaerium</i> sp.	Green
				<i>Fragilaria crotonensis</i>	Diatom
				<i>Gomphosphaeria</i> sp.	Blue-green
				<i>Melosira</i> sp.	Diatom
				<i>Stephanodiscus</i> sp.	Diatom

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20.0	12.2	11.4	<i>Aphanizomenon flos-aquae</i>	Blue-green
			<i>Fragilaria crotonensis</i>	Diatom
			<i>Gomphosphaeria</i> sp.	Blue-green
			<i>Melosira</i> sp.	Diatom
			<i>Stephanodiscus</i> sp.	Diatom
37.0	12.1	11.6	<i>Dictyosphaerium</i> sp.	Green
			<i>Fragilaria crotonensis</i>	Diatom
			<i>Gomphosphaeria</i> sp.	Blue-green
			<i>Melosira</i> sp.	Diatom
			<i>Stephanodiscus</i> sp.	Diatom

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*\*Blue-green algae present but not dominant*